

## Term Information

Effective Term Autumn 2016

## General Information

Course Bulletin Listing/Subject Area Mathematics  
Fiscal Unit/Academic Org Mathematics - D0671  
College/Academic Group Arts and Sciences  
Level/Career Graduate  
Course Number/Catalog 7221.02  
Course Title Ergodic Theory I  
Transcript Abbreviation Ergodic Theory 1  
Course Description Measure preserving transformations; isomorphism, conjugacy, spectral isomorphism; measure preserving systems with discrete spectrum; hierarchy of mixing properties; invariant measures for continuous transformations; topological and symbolic dynamics.  
Semester Credit Hours/Units Fixed: 3

## Offering Information

Length Of Course 14 Week  
Flexibly Scheduled Course Never  
Does any section of this course have a distance education component? No  
Grading Basis Satisfactory/Unsatisfactory  
Repeatable No  
Course Components Lecture  
Grade Roster Component Lecture  
Credit Available by Exam No  
Admission Condition Course No  
Off Campus Never  
Campus of Offering Columbus

## Prerequisites and Exclusions

Prerequisites/Corequisites By permission of the instructor. This course section is open only to mathematics post-candidacy students.

Exclusions

## Cross-Listings

Cross-Listings

## Subject/CIP Code

Subject/CIP Code 27.0101  
Subsidy Level Doctoral Course  
Intended Rank Doctoral

## Requirement/Elective Designation

The course is an elective (for this or other units) or is a service course for other units

## Course Details

### Course goals or learning objectives/outcomes

- Students will acquire the theoretical understanding and problem solving skills in ergodic theory that will enable them to use techniques in this field in conducting mathematical research in related areas.

### Content Topic List

- Measure preserving transformations
- Isomorphism, conjugacy and spectral isomorphism
- The hierarchy of mixing properties
- Invariant measures for continuous transformations
- Topological dynamics
- Symbolic dynamics

## Attachments

- MATH\_7221.02\_Syllabus.pdf: 7221.02 Syllabus

*(Syllabus. Owner: Kerler,Thomas)*

## Comments

- This course request relates to our course change request for Math 7221.01.  
(See that request for explanations and rationale) *(by Kerler,Thomas on 11/30/2015 09:59 PM)*

## Workflow Information

Status	User(s)	Date/Time	Step
Submitted	Kerler,Thomas	12/01/2015 02:07 PM	Submitted for Approval
Approved	Husen,William J	12/01/2015 02:11 PM	Unit Approval
Approved	Haddad,Deborah Moore	12/01/2015 02:59 PM	College Approval
Pending Approval	Nolen,Dawn Vankeerbergen,Bernadette Chantal Hanlin,Deborah Kay Jenkins,Mary Ellen Bigler Hogle,Danielle Nicole	12/01/2015 02:59 PM	ASCCAO Approval

---

---

# Ergodic Theory 1

---

---

## Instructor and Class Information

---

Lecturer:	Course Num.:
Office:	Lecture Room:
Phone:	Lecture Times:
Email:	Office Hours:

## About Course Goals

---

### FORMAT

The course will meet three times a week for 55 minutes each meeting. Instruction will be mainly by lecture delivered by the instructor. It may also include occasional in-class discussions as well as short student presentations, particularly, by post-candidacy students.

### DESCRIPTION & GOALS

This course sequence is aimed at providing students with a solid working knowledge in the basic concepts, important techniques and examples in Ergodic Theory, and constitutes a natural continuation of the Math 6211-6212 sequences in Real Analysis. The course should be of interest to all students with research interests in various flavors of ergodic theory and dynamical systems, and its applications to study problems in Combinatorics, Number theory, Homegeneous Dynamics, Differential equations, Probability theory etc.

### PREREQUISITES

This section is open only to mathematics post-candidacy students and requires, in addition, the permission of the instructor.

## Textbook

---

### MAIN REFERENCE

Peter Walters, "*An Introduction to Ergodic theory*". Graduate Texts in Mathematics **79**, Springer 2000, ISBN-13: 978-0387951522.

### ADDITIONAL REFERENCES

Karl E. Petersen, "*Ergodic Theory*". Cambridge Studies in Advanced Mathematics **2**, Cambridge University Press 1990, ISBN-13: 978-0521389976.

M. Einsiedler and T. Ward: "*Ergodic theory: with a view towards Number Theory*". Graduate Texts in Mathematics **259**, Springer 2010, ISBN-13: 978-0857290205.

## Assessments

---

### READING, PARTICIPATION, AND ATTENDANCE

Students are required to read scheduled textbook materials and actively participate in class room discussions that arise from lecture material. Students are expected to attend all classes.

## RESEARCH ORIENTED PRESENTATION

Post-candidacy students in this section are required to deliver a half hour presentation that both synthesizes lecture material and connects it to relevant research questions, more advanced theoretical topics, or applications in other fields of mathematics. The topic and required independent reading will be determined by the instructor individually in negotiation with the student. Presentations may also be replaced by respective research papers upon the request of the student.

## Grading

---

### COURSE GRADE

This course section is graded satisfactory/unsatisfactory. A satisfactory outcome will require continued active participation in class (weighed about 20%) and be further based on the student's performance during the presentation (weighed about 80%).

## Weekly Schedule

---

Week 1	Review of $\sigma$ -algebras, measure theory, function spaces, Spectral theorem etc.
Week 2	Measure preserving transformations, Recurrence, Variety of examples
Week 3	Basic constructions, Ergodicity criteria, Verification techniques in examples
Week 4	The Ergodic theorems –Maximal ergodic theorem, Pointwise ergodic theorem, Mean Ergodic Theorem
Week 5	Applications of ergodic theorems and examples
Week 6	Mixing and weak mixing criteria, Verification techniques, and Examples
Week 7	Isomorphism, conjugacy, spectral isomorphism, discrete spectrum
Week 8	Basics of Entropy theory
Week 9	Methods of calculating entropy and examples
Week 10	Topological Dynamics
Week 11	Invariant measures for Continuous transformations
Week 12	Topological Entropy and Information, Calculation of topological entropy
Week 13	The variational principle, Entropy of affine transformation,
Week 14	Miscellaneous topics

## General Policies

---

### ACADEMIC MISCONDUCT

It is the responsibility of the Committee on Academic Misconduct to investigate or establish procedures for the investigation of all reported cases of student academic misconduct. The term “academic misconduct” includes all forms of student academic misconduct wherever committed; illustrated by, but not limited to, cases of plagiarism and dishonest practices in connection with examinations. Instructors shall report all instances of alleged academic misconduct to the committee (Faculty Rule 3335-5-487). For additional information, see the Code of Student Conduct ([http://studentaffairs.osu.edu/info\\_for\\_students/csc.asp](http://studentaffairs.osu.edu/info_for_students/csc.asp)).

**DISABILITY SERVICES**

Students with disabilities that have been certified by the Office for Disability Services will be appropriately accommodated and should inform the instructor as soon as possible of their needs. The Office for Disability Services is located in 150 Pomerene Hall, 1760 Neil Avenue; telephone 292-3307, TDD 292-0901; <http://www.ods.ohio-state.edu/>.